

Molecular Mechanic/ Poisson-Boltzmann Surface Area (MM/PBSA)

Biophysics 206

Spring 2004

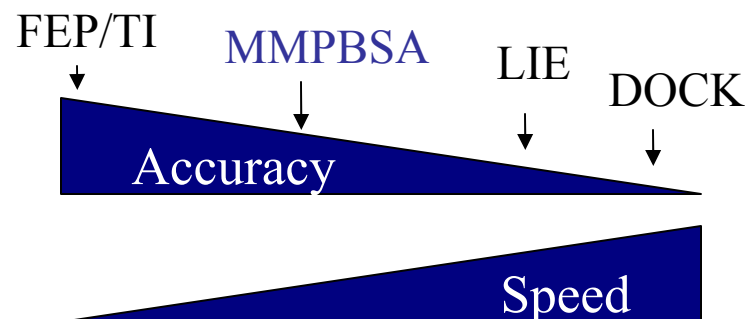
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MMPBSA

- Molecular Mechanics/ Poisson-Boltzmann Surface Area (MM/PBSA)
- MM = internal energy of the system (BADH and NB)
- PB = electrostatic contribution to solvation
- SA = nonpolar contribution to solvation
- S = entropic contribution to binding
- Files needed :
 1. Topology files for all components (R, L, RL)
 2. Trajectory file (coordinates)

MMPBSA background

- Co-Developed by Dave Case (Scripps) and Peter Kollman (UCSF)
 - First successful implementation Srinivasan (1998) JACS 120(37), 9401-9409.
- Generalizable
- Molecular dynamics used in conjunction with free energy calculation methods can yield energetic determinants to binding.

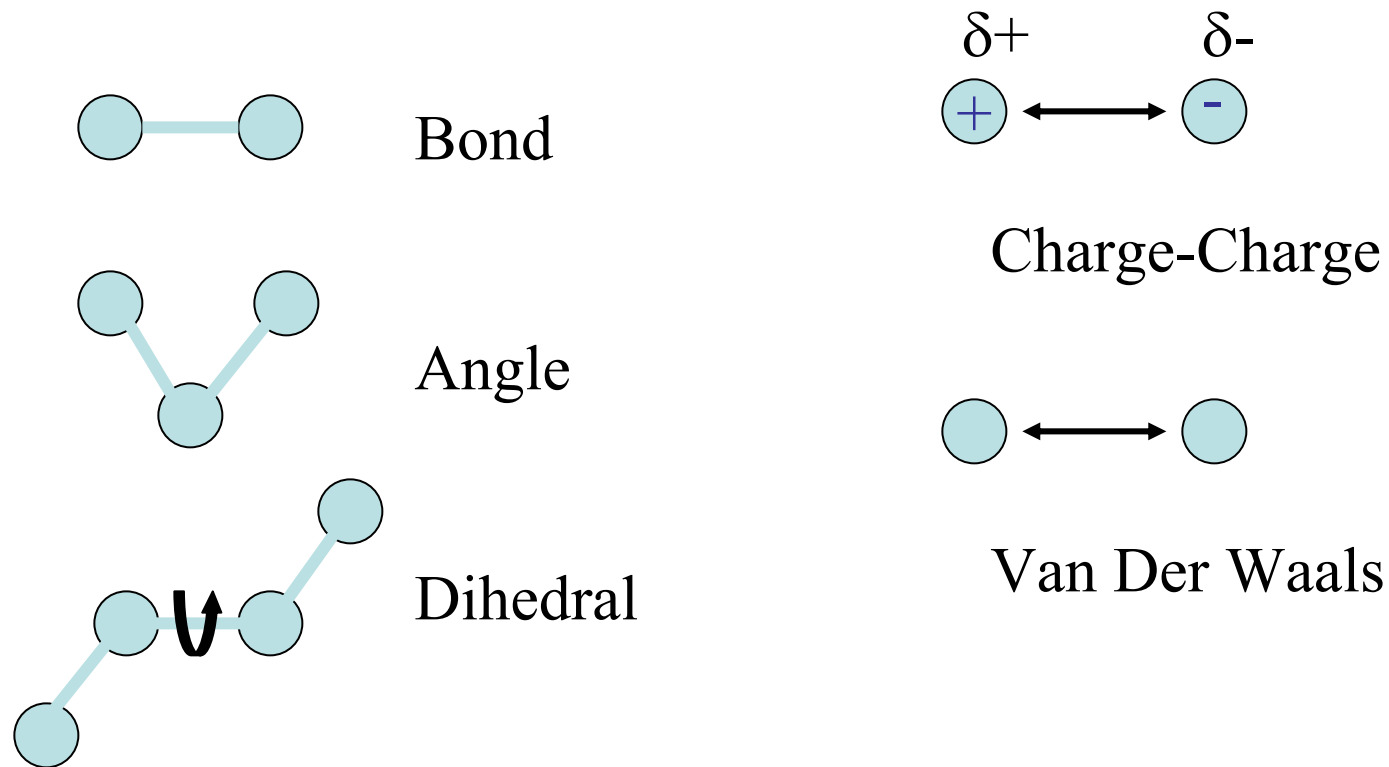


- Advantage over FEP: can take into account large structure changes
 - Calculates G at endpoints, don't sample intermediates
 - But errors larger, still get good agreement with experiment
 - Continuum solvent has integrated out solvent coords

Methodology

1. Use MD to generate a representative set of structures
 2. Representative snapshots taken from the trajectory at fixed intervals (5ps or 10ps intervals)
 3. Post-process these structures removing solvent
 4. Obtain free energy
- Takes advantage of multiple snapshots from a trajectory to get an average of energies

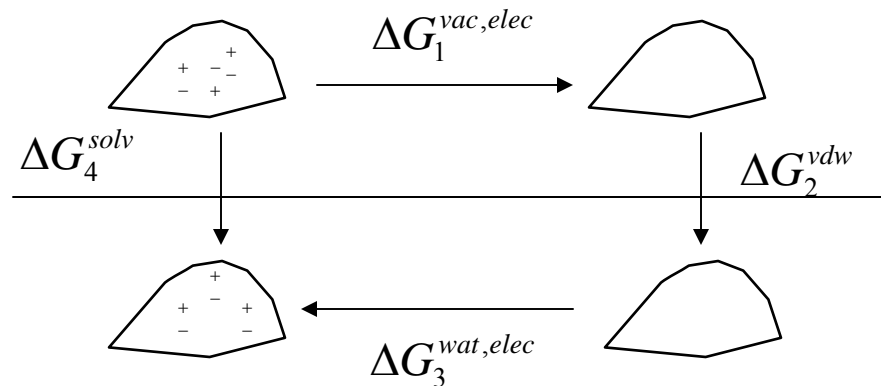
Molecular Mechanics (MM)



$$V(\mathbf{r}^N) = \sum K_r (l - l_{eq})^2 + \sum K_\theta (\theta - \theta_{eq})^2 + \sum \frac{1}{2} V_n (1 + \cos(n\omega - \gamma)) +$$

$$(\sum 4e_{ij} [(\sigma/r_{ij})^{12} - (\sigma/r_{ij})^6] + qq/4\pi\epsilon r_{ij})$$

Poisson-Boltzmann Surface Area (PBSA)*



- Poisson-Boltzmann for electrostatic solvation energies
- Change in solvent accessible surface area for nonpolar solvation energies

$$\Delta G_{electrostatics} = \frac{1}{2} \sum q_i (\phi_i^{80} - \phi_i^1)$$

$$\Delta G_{solv}^{nonpolar} = \gamma(SASA) + b$$

$$\begin{aligned} \gamma &= 0.00542 \text{ kcal/mol } \text{\AA}^2 \\ b &= 0.92 \text{ kcal/mol} \end{aligned}$$

*Sitkoff, JPC 1994, 98(7) 1978-1988

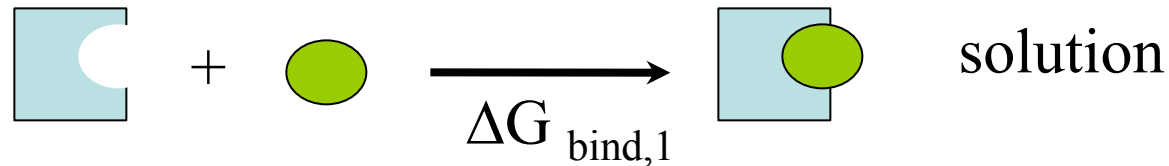
Entropy ($T\Delta S$)

- Many times ignored if ligands all roughly the same size
- Time intensive calculation for very little added information

- Normal Mode (NM)
 - Long minimization time to get tight convergence.

- Quasi-harmonic
 - Need long MD times

One snapshot



$$\Delta \bar{G}_{bind,1} = \Delta \bar{E}_{MM} + \Delta \bar{G}_{Solv}^{PBSA} - T\Delta \bar{S} \quad (1)$$

$$\Delta E_{MM} = (E_{MM}^{complex} - E_{MM}^{Receptor} - E_{MM}^{Ligand})$$

$$\Delta G_{solvation} = (\Delta G_{solv}^{complex} - \Delta G_{solv}^{Receptor} - \Delta G_{solv}^{Ligand})$$

$$\Delta S = (S^{complex} - S^{Receptor} - S^{Ligand})$$

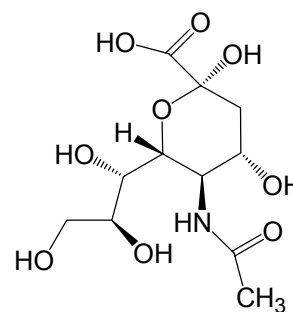
$$\bar{E}_{MM} = \bar{E}_{Bond} + \bar{E}_{Angle} + \bar{E}_{torsion} + \bar{E}_{VDW} + \bar{E}_{Elec}$$

$$\Delta \bar{G}_{solv}^{PBSA} = \Delta \bar{G}_{solv}^{nonpolar} + \Delta \bar{G}_{solv}^{electrostatic}$$

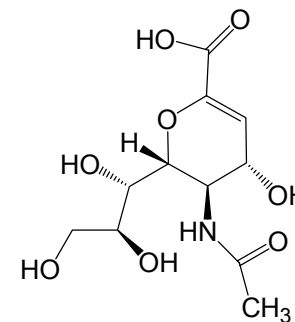
$$\Delta \Delta G_{Bind} = \Delta G_{Bind,1} - \Delta G_{Bind,2} \quad (2)$$

Neuraminidase study

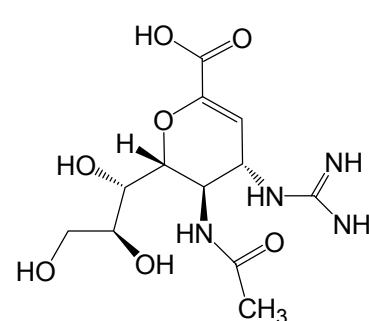
- Structurally similar, but bind with large variation in free energy
- Four co-crystal structures



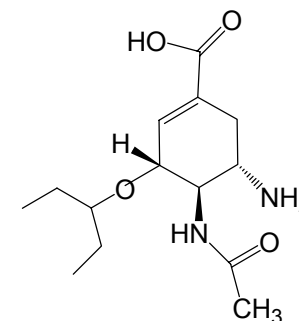
Sialic Acid



DANA



Relenza



Tamiflu

Sialic Acid	-2.76 kcal/mol
DANA	-6.91 kcal/mol
Relenza	-13.2 kcal/mol
Tamiflu	-15.2 kcal/mol

Interaction Energies

Contribution	Tamiflu	Relenza	DANA	Sialic Acid
ΔE internal ^[1]	-6.07 (0.51)	1.90 (0.68)	-5.36 (0.53)	5.16 (0.48)
ΔE vDW ^[2]	-29.16 (0.48)	-29.99 (0.51)	-23.13 (0.56)	-23.32 (0.47)
ΔE elect, internal ^[3]	-44.49 (0.52)	-58.49 (0.39)	-35.15 (0.53)	-44.91(0.28)
ΔG elect,solv ^[4]	46.81 (0.42)	58.22 (0.27)	38.46 (0.39)	45.4(0.21)
ΔG nonpolar, solv ^[5]	-4.46 (0.01)	-4.65 (0.01)	-4.12 (0.01)	-4.13 (0.01)
ΔE Elec, int+solv ^[6]	2.31 (0.17)	-0.26 (0.22)	3.31 (0.24)	0.49 (0.21)
$-T\Delta S$ ^[7]	21.6 (1.35)	19.6 (1.56)	22.4 (1.64)	20.11 (1.47)
ΔG bind ^[8]	-15.78 (1.49)	-13.4 (1.63)	-6.90 (1.70)	-1.69 (1.58)

^[1] Internal contributions from bond, angle, and dihedral terms

^[2] Non-bonded van der Waals

^[3] Non-bonded electrostatics

^[4] Non-polar and electrostatic components to solvation

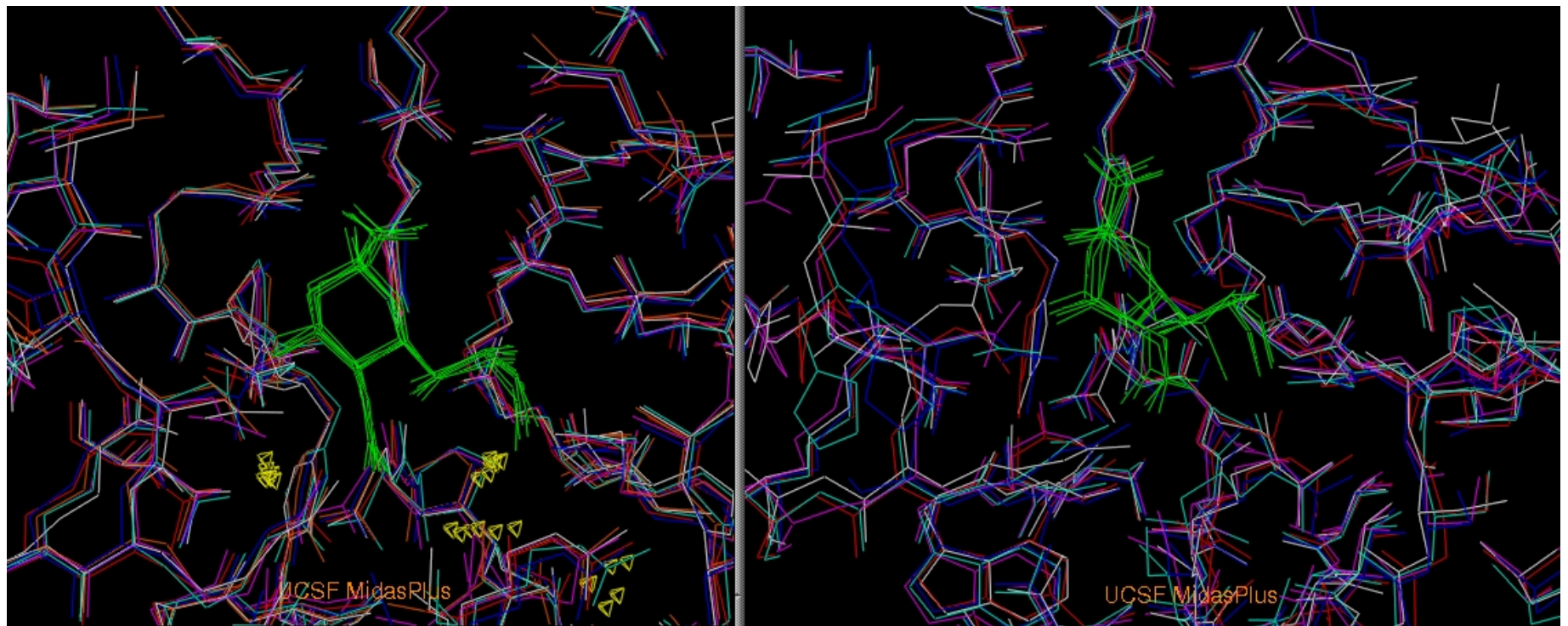
^[5] Electrostatic components to solvation

^[6] Total electrostatic change upon binding

^[7] Entropic contributions to binding

^[8] Total change of free energy in binding

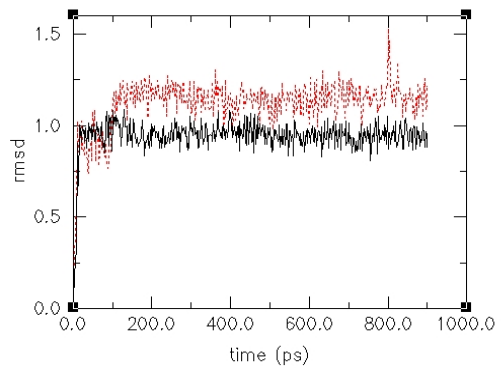
SIA structure overlay



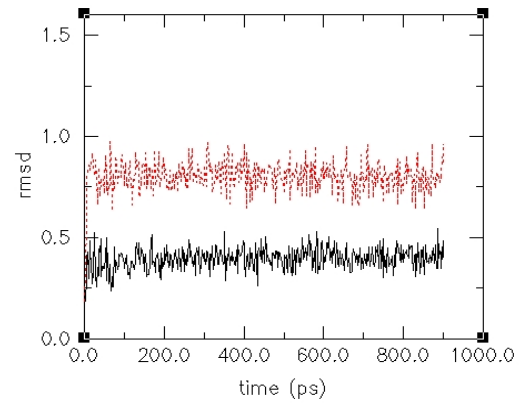
Simulation w/ crystal waters

Simulation without

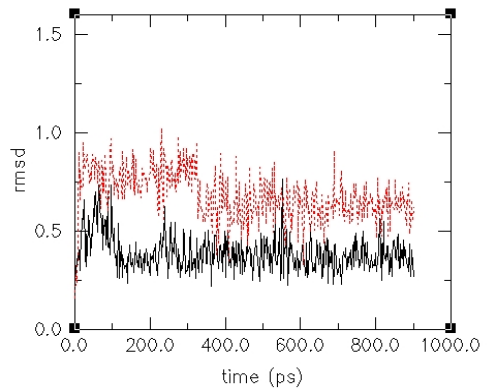
Ligand RMSD During Simulations



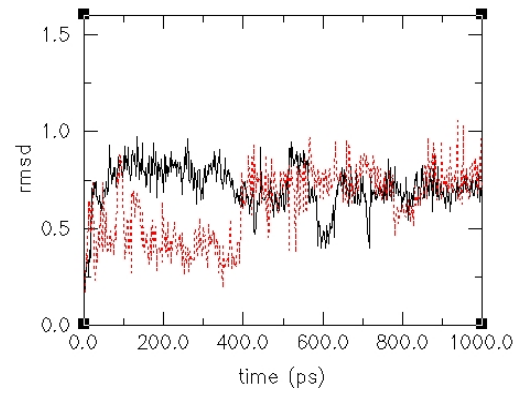
Sialic Acid



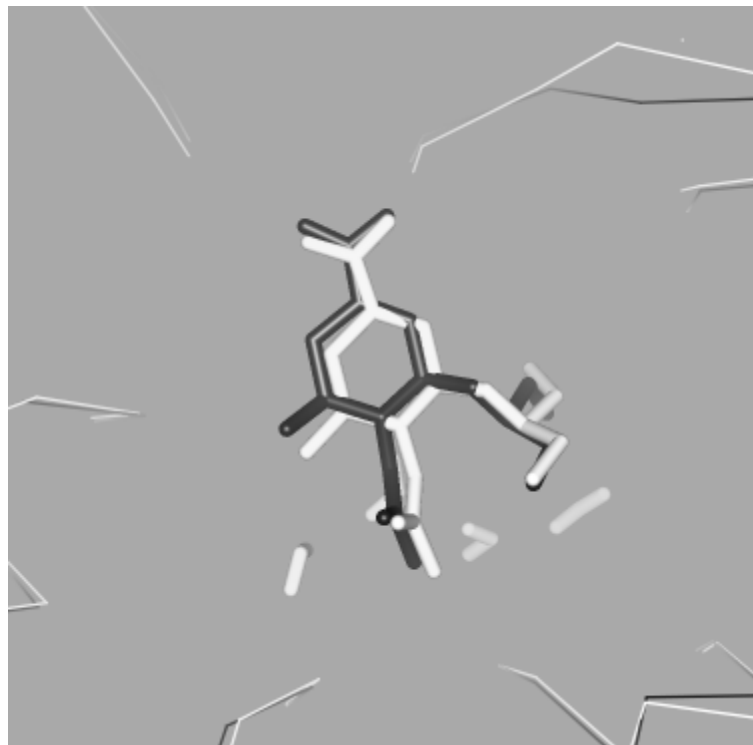
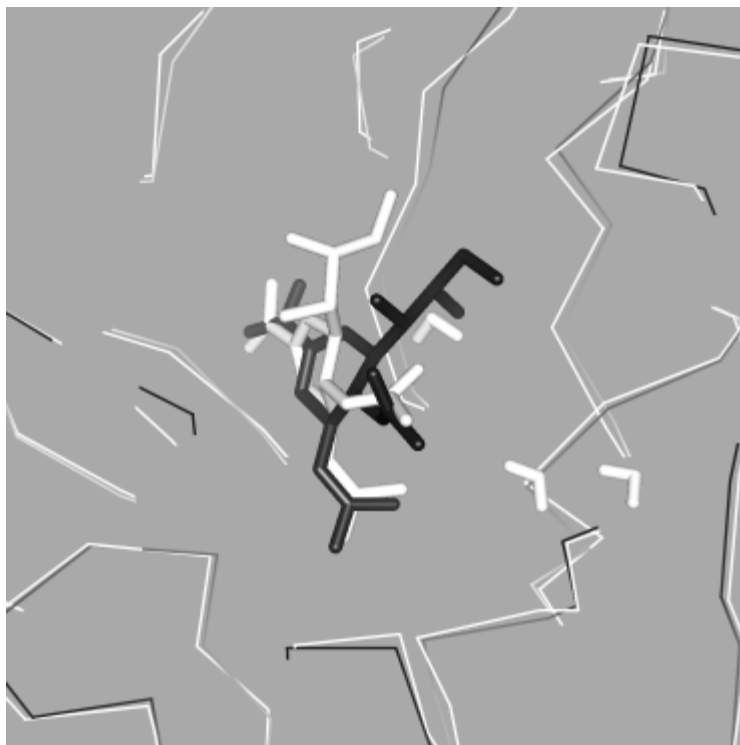
Relenza



DANA

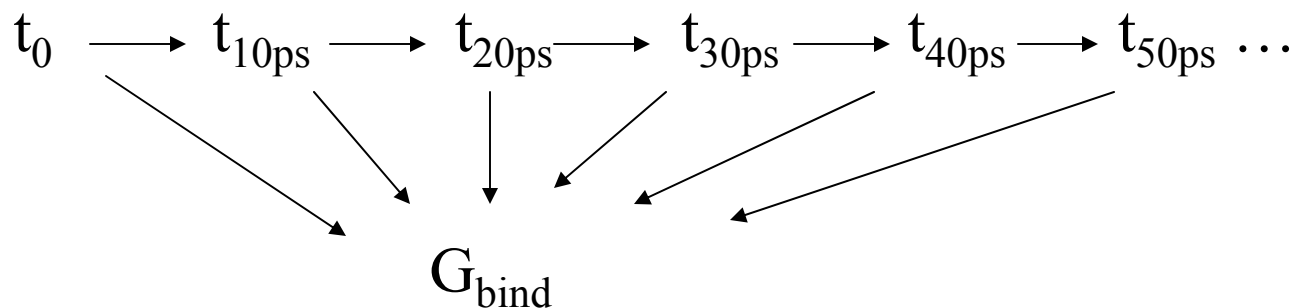


Tamiflu



MM/PBSA overview

- Combines molecular dynamics and a free energy scoring scheme to get free energies of binding
 - Free energy of binding determined via Molecular Mechanic/Poisson-Boltzmann Surface Area scoring function (MM/PBSA)

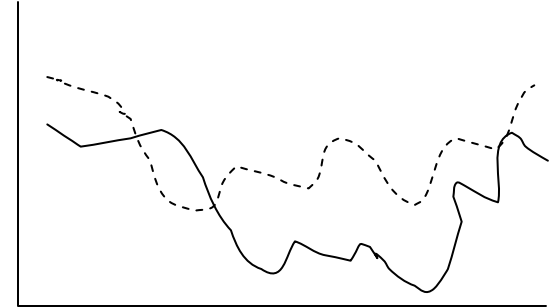


$$\Delta G_{bind} = \bar{G}_{complex} - (\bar{G}_{rec} + \bar{G}_{ligand})$$

$$\bar{G} = \bar{E}_{mm} + \bar{G}_{solv} - \bar{TS}$$

Caveats

- Errors (2-4 kcal/mol)
- Entropy
- Sampling landscape vs. MMPBSA landscape
- Sampling and Scoring



Some References

- MMPBSA overview
 - Srinivasan, *JACS* (1998) 120, 37,9401-9409
 - Cornell, *JACS* (1995) 117,19, 5179-5197
 - Kollman, *Accounts of Chem Research* (2000) 33(12); 889-897.
- Nucleic acid systems
 - Reyes, *RNA* (1999), 5, 235-244.
 - Cheatham, *JMB* (1996), 259, 434-444
- Structure prediction
 - Lee, *JACS*, (2001) 123(6); 1040-1046.
 - Duan, *Science* (1998), 282; 740-744.
- Binding
 - Kuhn, *J. Med. Chem.* (2000) 43(20); 3786-3791.
 - Chong, *PNAS* (1999), 96, 14330-14335.
 - Rizzo, *J. Med. Chem* (2004),47, 3065-3074
 - Masukawa, *J. Med. Chem.* (2004) 46(26); 5628-5637
- Alanine-scanning
 - Massova, *JACS* (1999), 121, 8133-8143